

Solid-state NMR : ~~targets~~ & methods

K. Takegoshi (Kyoto Univ.)

1) spin=1/2, rare spin, eg., ^{13}C , ^{15}N , ^{29}Si , ^{31}P , ^{113}Cd ,

δ_{iso} : high resolution NMR

δ_{CSA} : Chemical-shift anisotropy

Dipolar interactions : $^{13}\text{C}-^{13}\text{C}$, $^{13}\text{C}-^{15}\text{N}$

Cross polarization (CP)

Magic-angle spinning (MAS)

Dipolar decoupling&recoupling

2) spin=1/2, abundant spin, i. e., ^1H

δ_{iso} : high resolution NMR

Multiple pulse decoupling

CRAMPS

3) Half-integer spins, e. g. Al, Na, O...

δ_{iso} : high resolution NMR

δ_{CSA} : Chemical-shift anisotropy

Quadrupolar coupling

MQMAS, DOR, DAS . . .

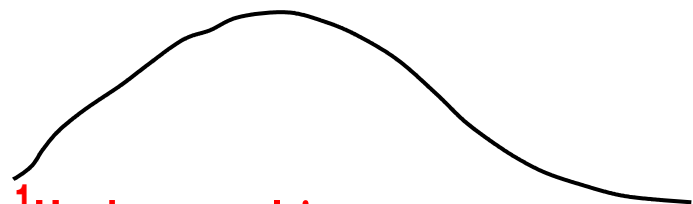
4) Integer spins, e. g. ^2H , ^{14}N

Quadrupolar coupling

***So far, no practical methods
for high-resolution observation***

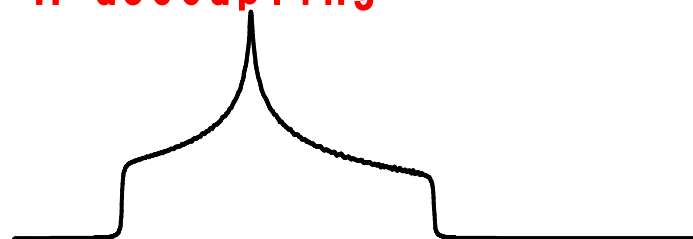
Powder NMR spectra of spin=1/2 (rare-nuclei case), eg. ^{13}C

No gadgets



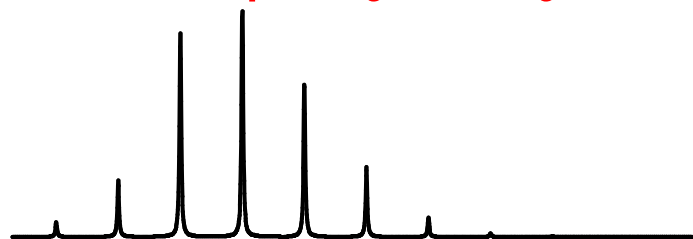
^{13}C chemical-shift anisotropy
 ^1H - ^{13}C heteronuclear dipolar interactions

^1H decoupling



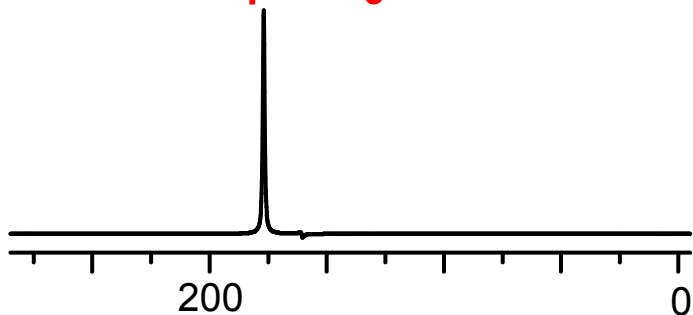
^{13}C chemical-shift anisotropy

^1H decoupling + Magic-angle spinning at 2 kHz



^{13}C isotropic shift + spinning sidebands

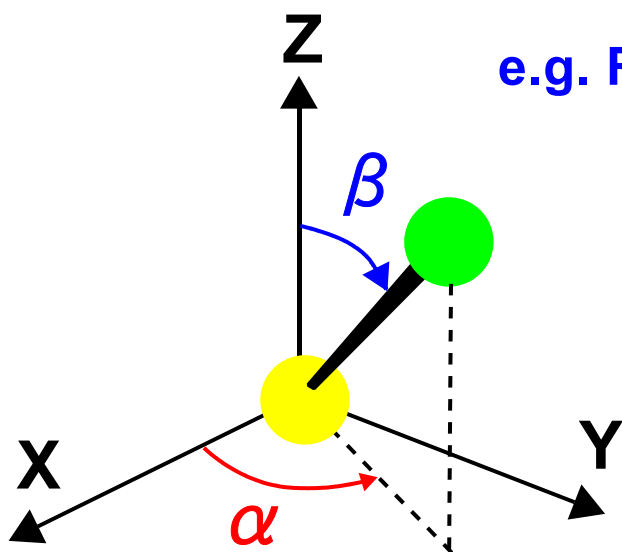
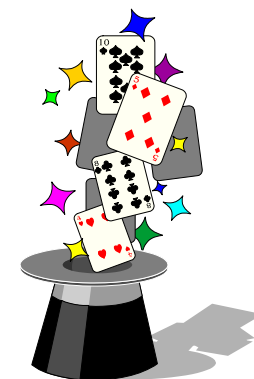
^1H decoupling + MAS at 20 kHz



^{13}C isotropic shift

Magic Angle Spinning

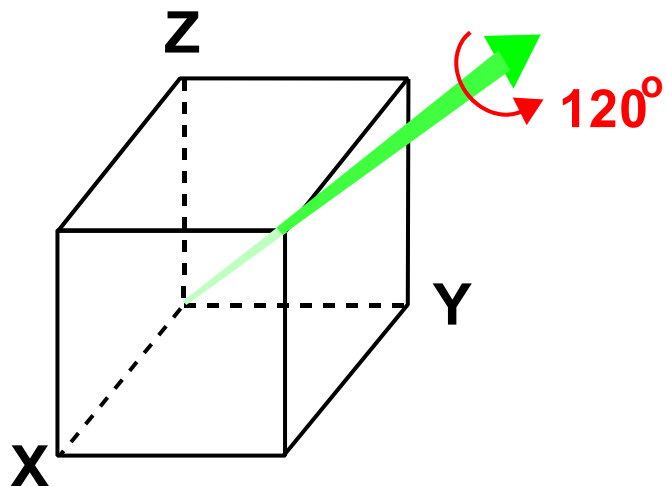
e.g. Removal of dipolar broadening by MAS



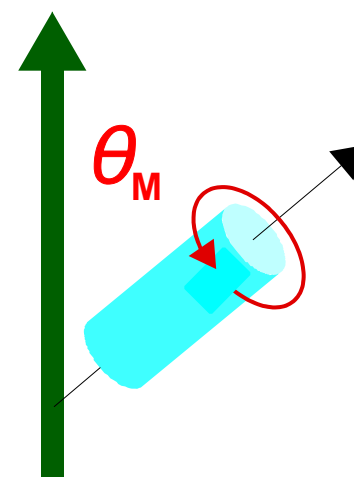
$$B // Z \quad d_z \propto 3 \cos^2 \beta - 1$$

$$B // X \quad d_x \propto 3 \sin^2 \beta \cos^2 \alpha - 1$$

$$B // Y \quad d_y \propto 3 \sin^2 \beta \sin^2 \alpha - 1$$

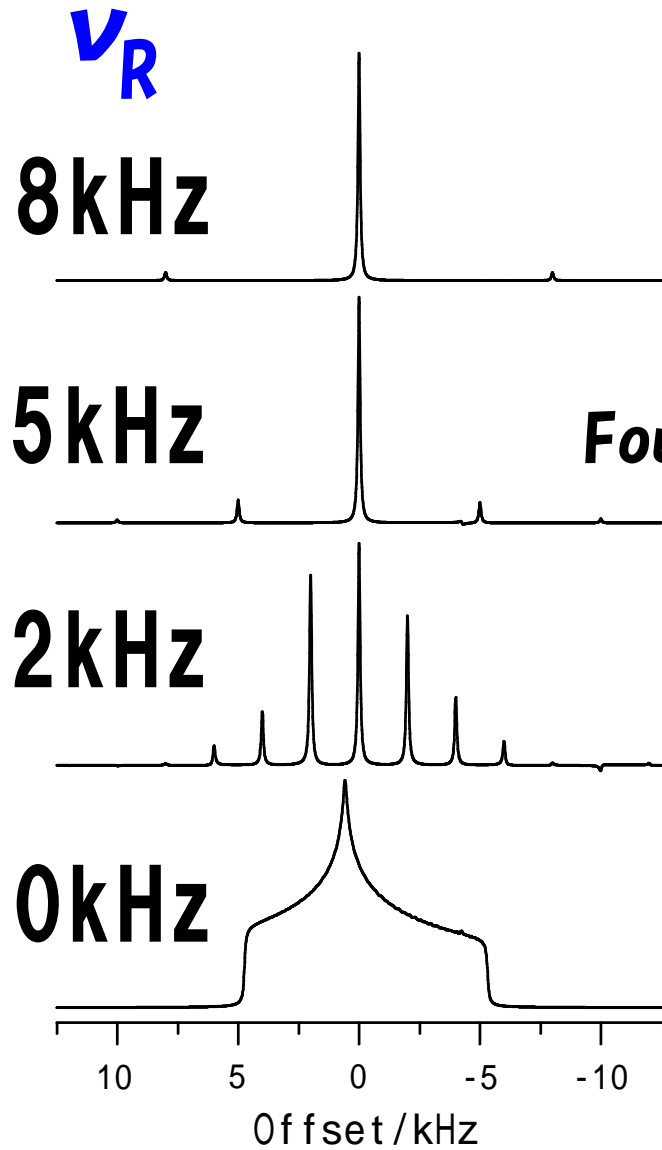


$$d_x + d_y + d_z = 0 !!$$

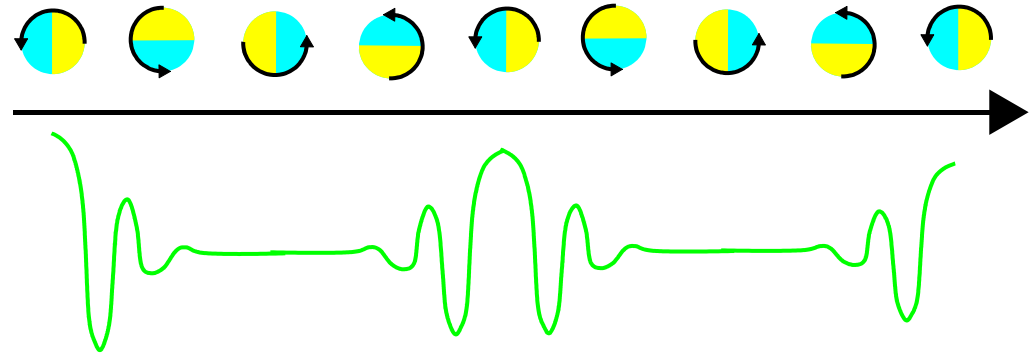
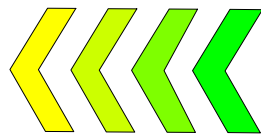


Spinning sidebands

$\nu_R \gg$ Chemical shift anisotropy
 $\propto B_0$

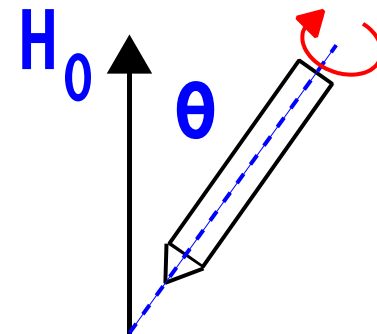


Fourier transform

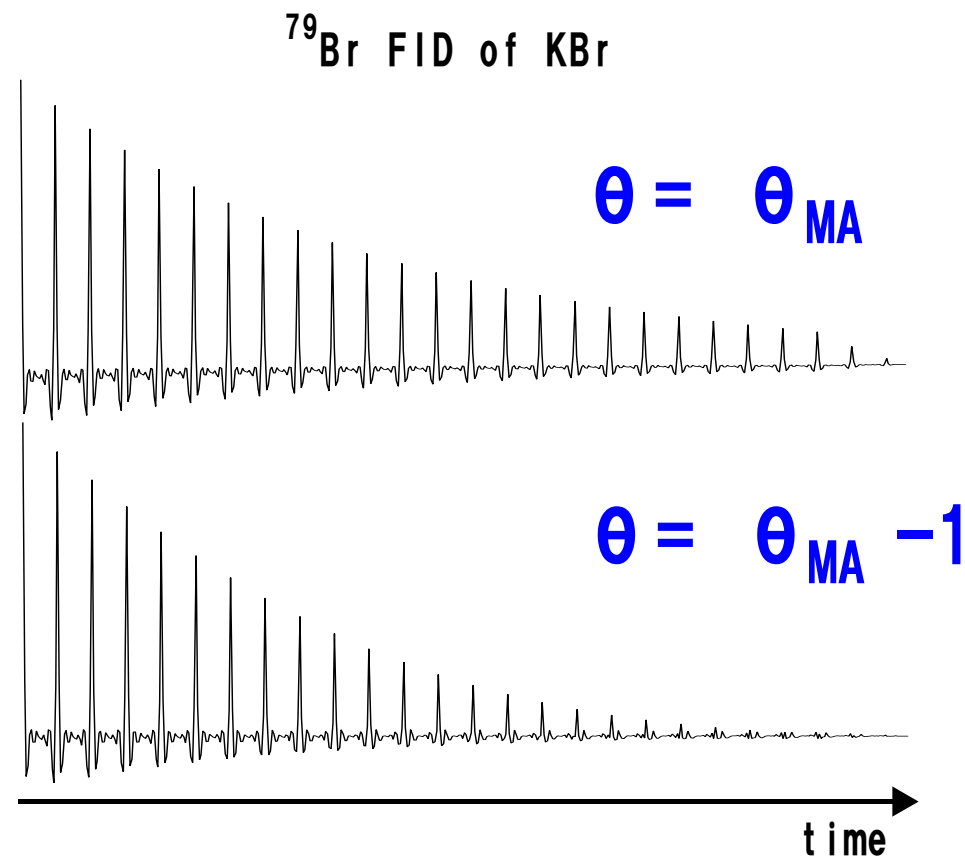
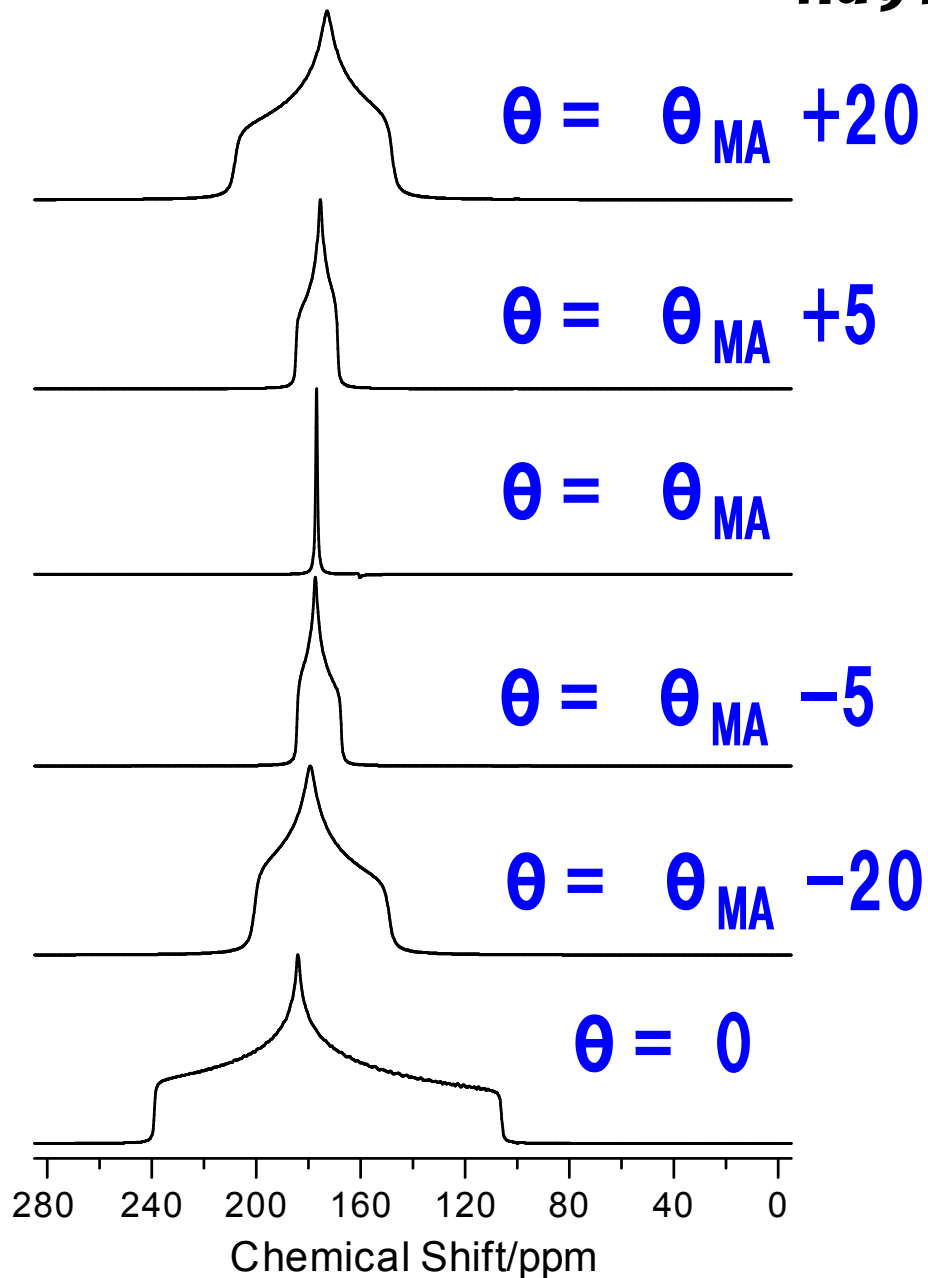


Rotational echo

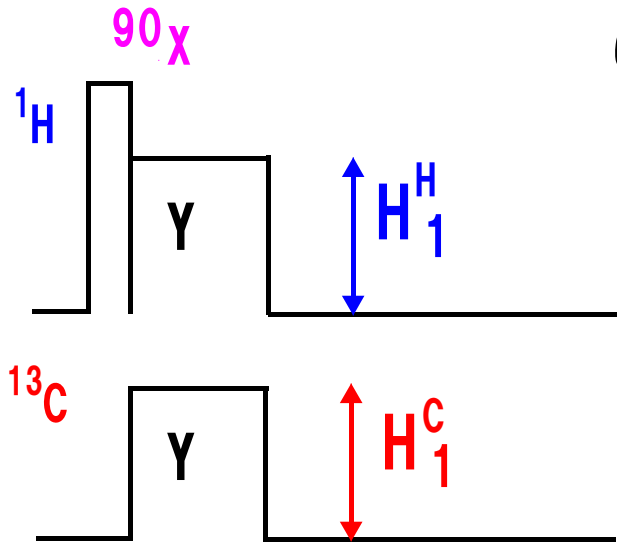
Magic angle ...



One has to adjust the angle precisely!



Cross polarization (CP)

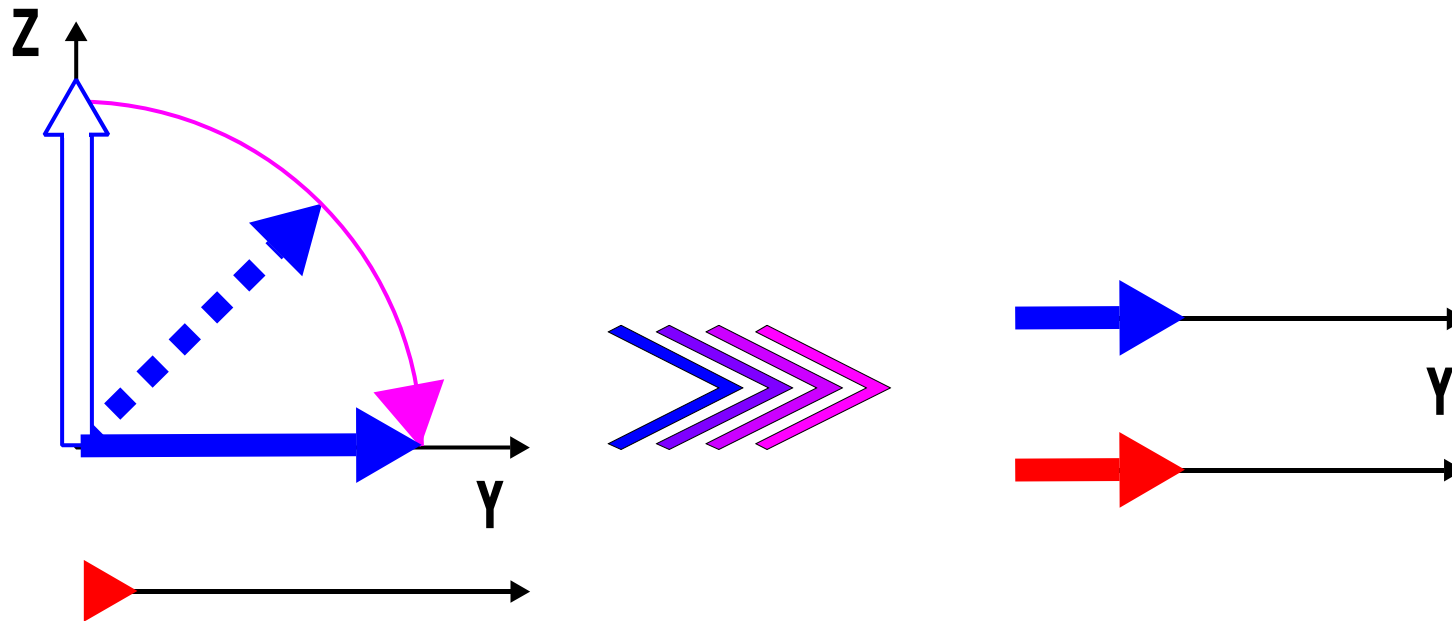


$$\gamma_H H_1^H = \gamma_C H_1^C$$

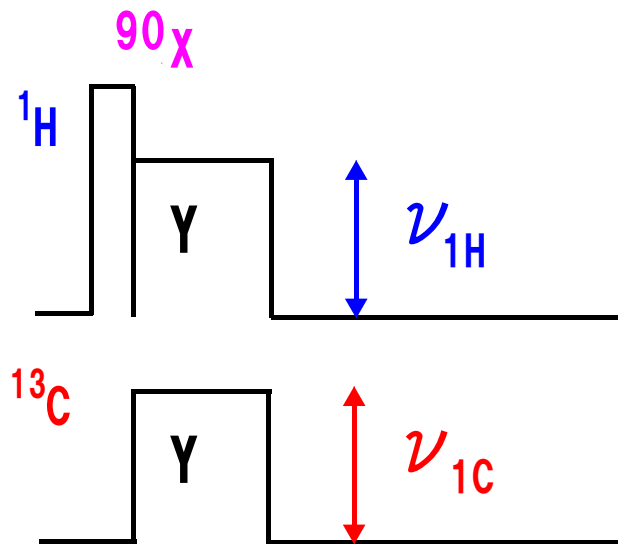
Hartman-Hahn condition
(H_1 : Tesla)

$$\nu_{1H} = \nu_{1C}$$

H-H in Frequency unit

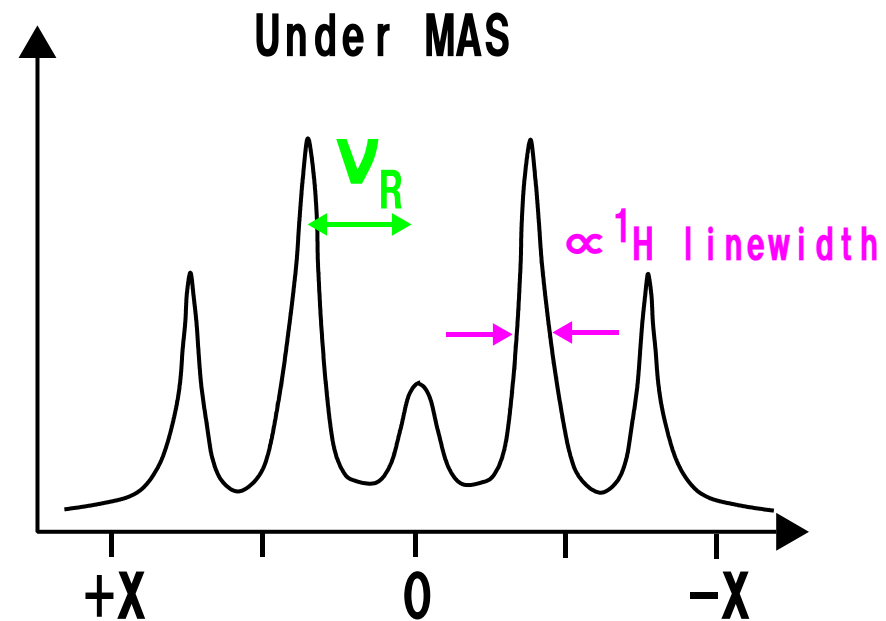
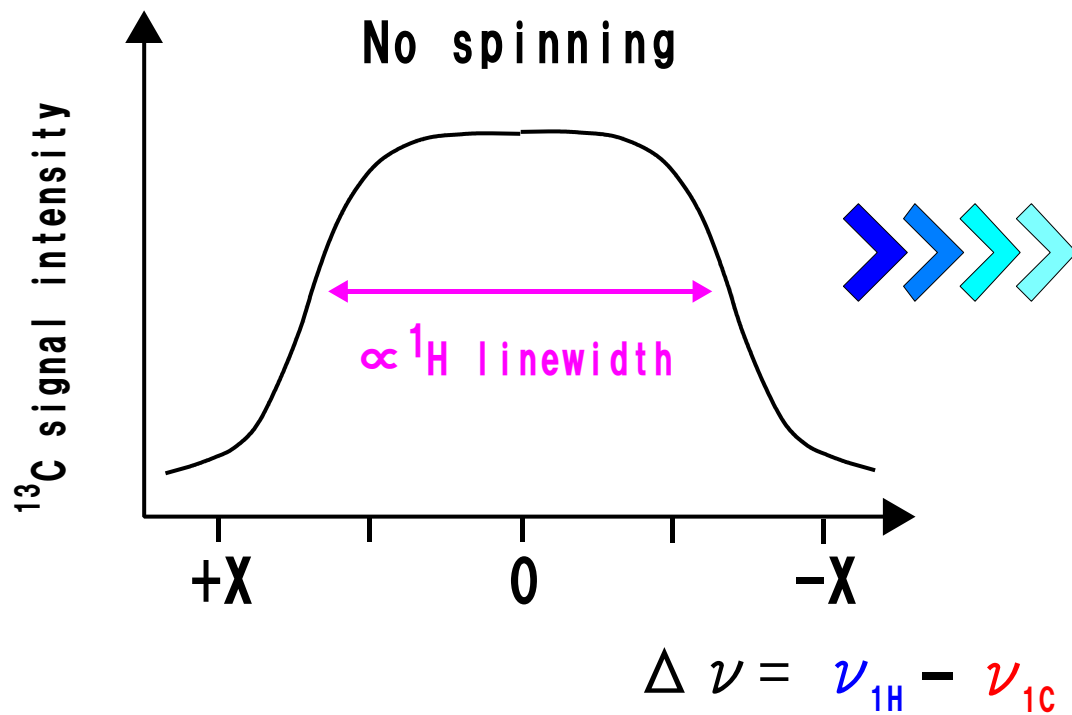


Effect of MAS on CP



H-H condition under MAS

$$\nu_{1\text{H}} = \nu_{1\text{C}} + n \nu_{\text{R}}$$



CP under MAS

For the on-resonance spin

$$\nu_{1H} = \nu_{1C} + n\nu_R$$

For the off-resonance spins

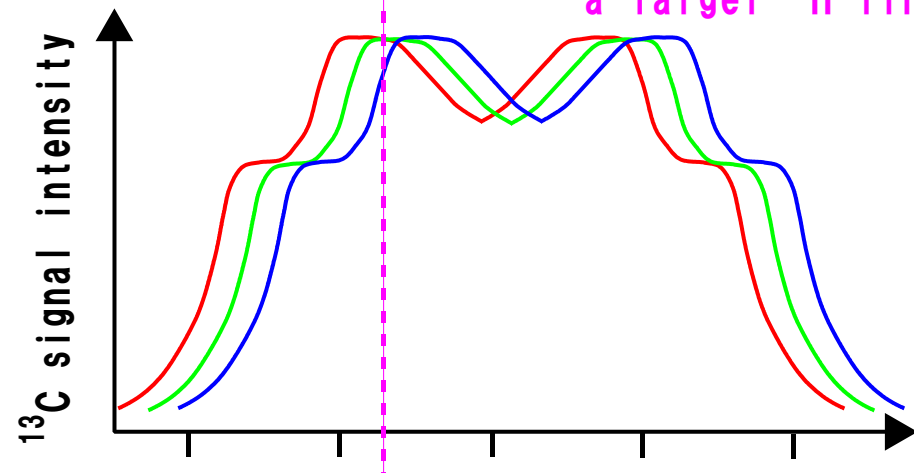
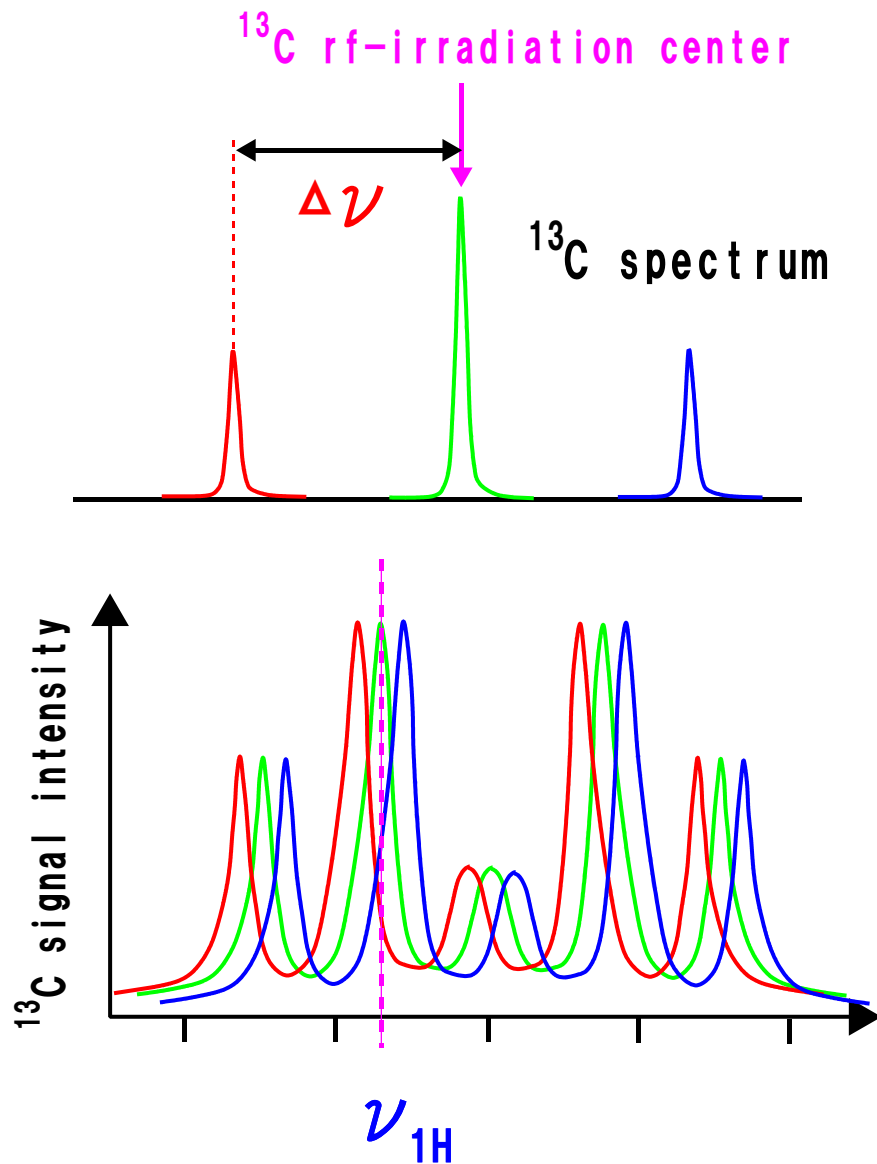
$$\nu_{1H} \neq \nu_{1C}^{eff} + n\nu_R$$

Effective field

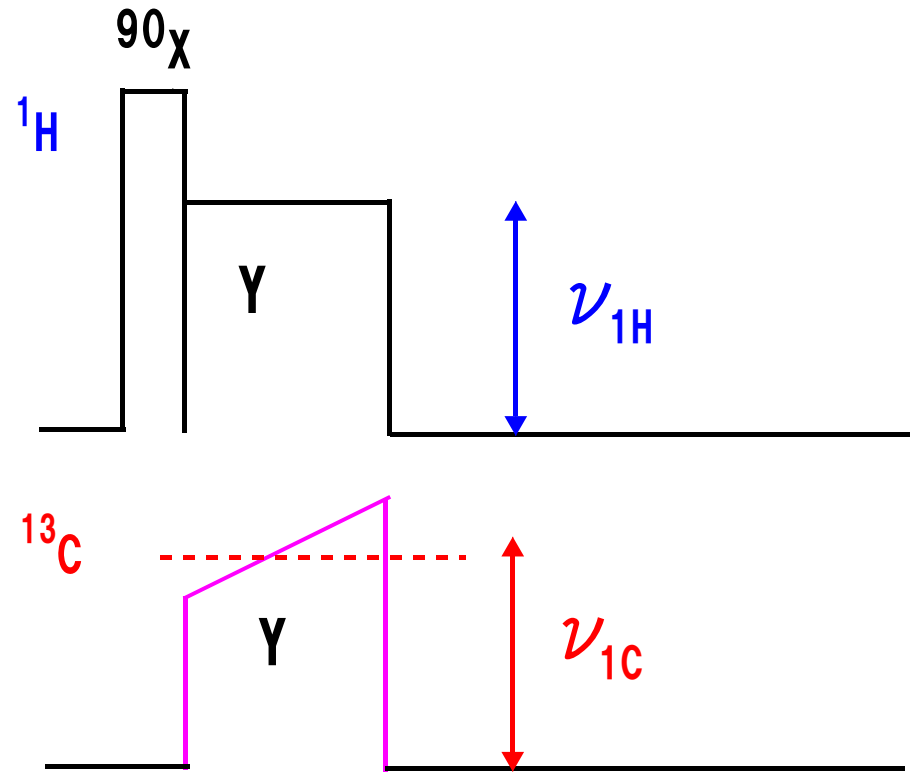
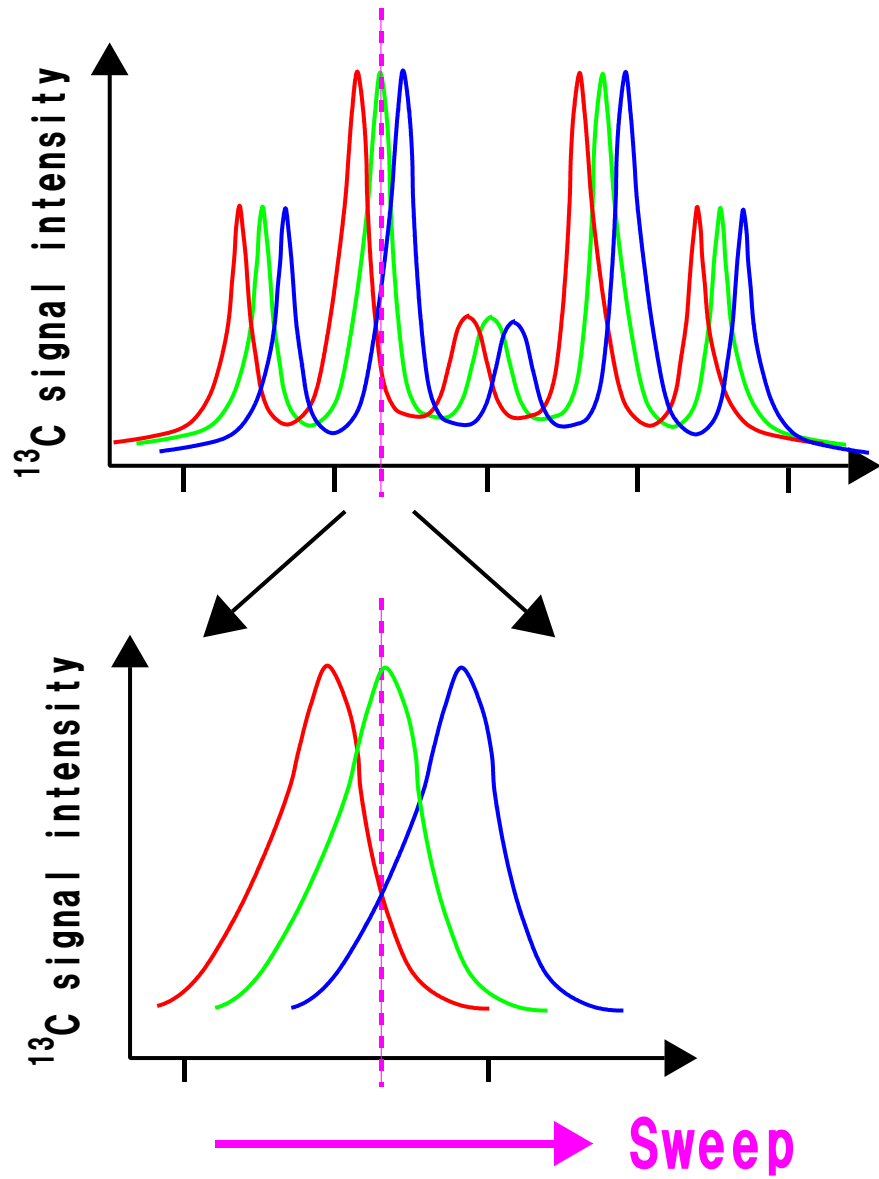
$$|\nu_X^{eff}| = \sqrt{\nu_{1X}^2 + \Delta\nu_X^2}$$

For a rigid system

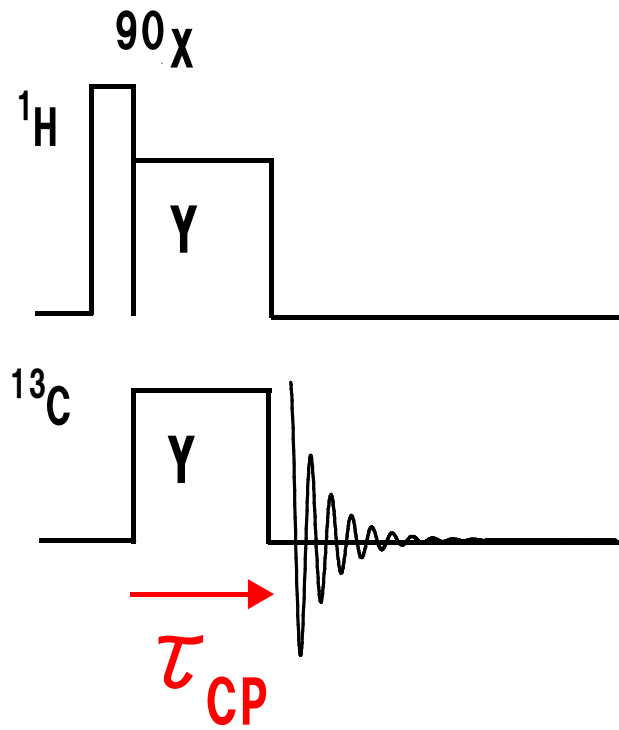
a larger 1H linewidth



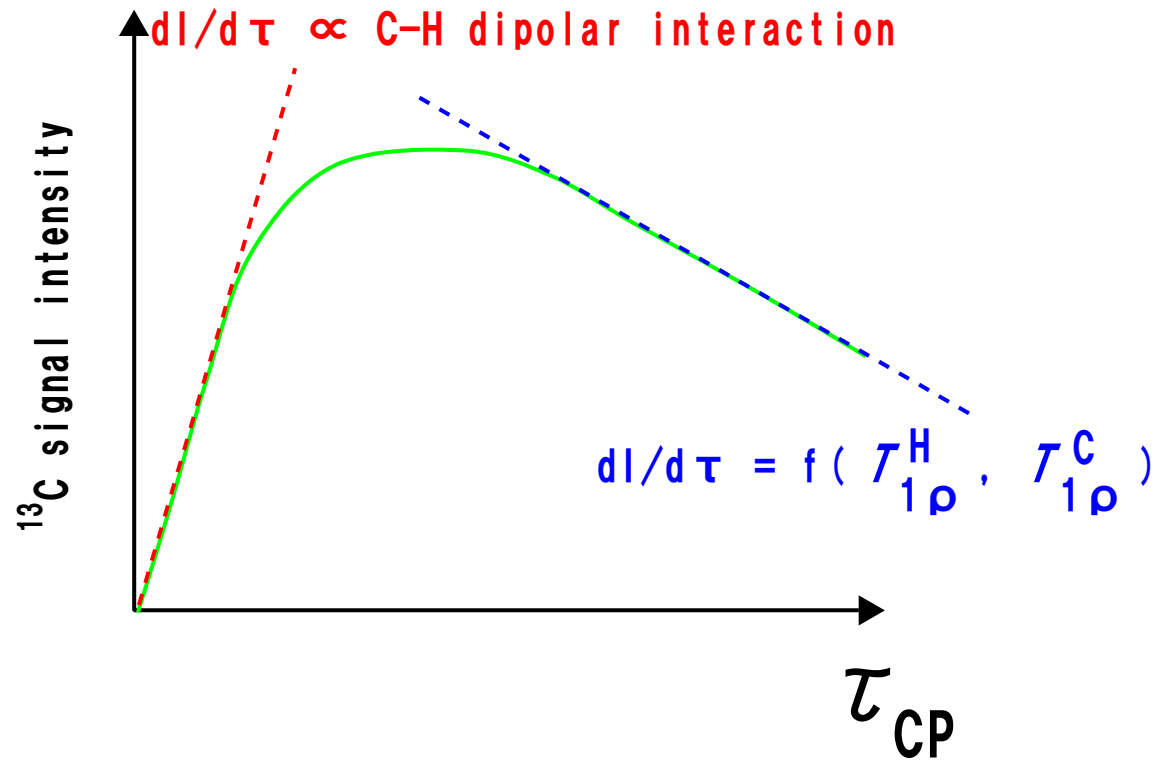
Ramped CP under MAS



CP dynamics



contact time

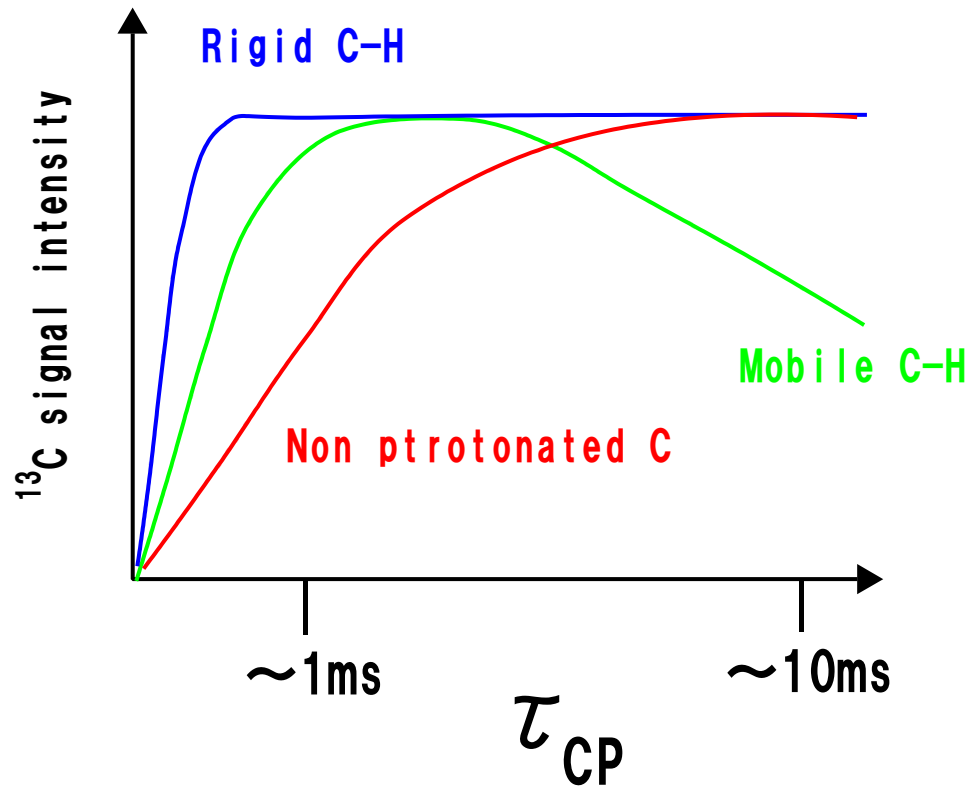
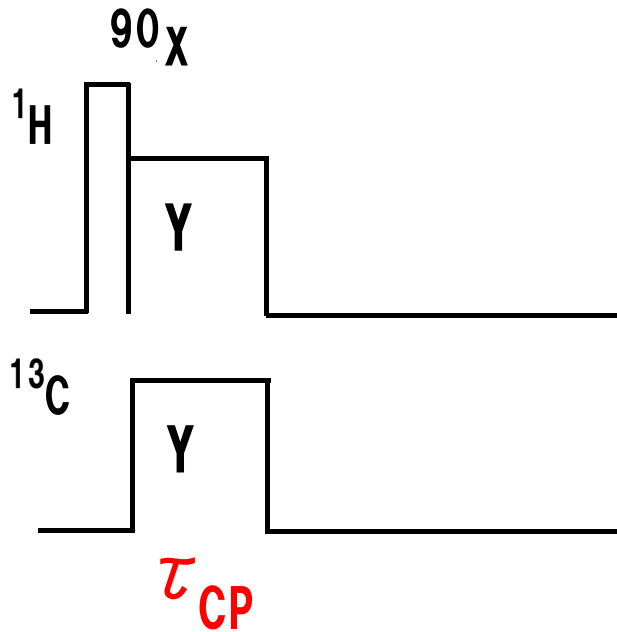


For a rigid C-H : **quick buildup**

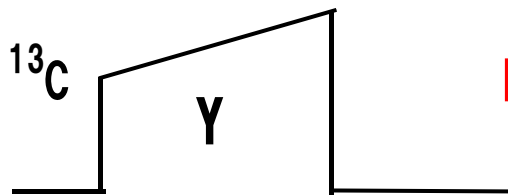
Motional frequency $\sim \nu_1$: Short $T_{1\rho}$

→ **quick decay**

Optimal contact time

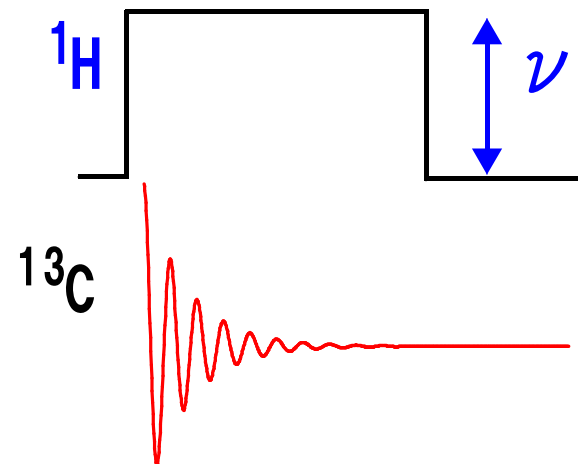
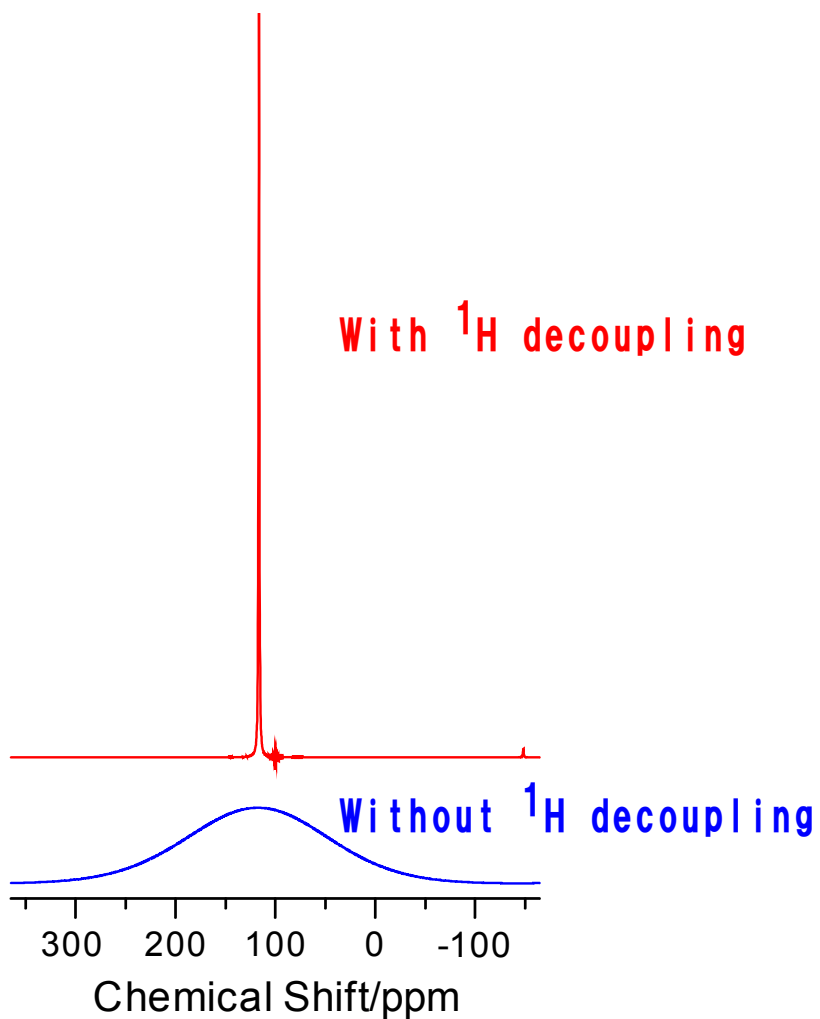


Note! Ramp CP requires a longer contact time!



Mind if your C-H system has short $T_{1\rho}$

^1H decoupling

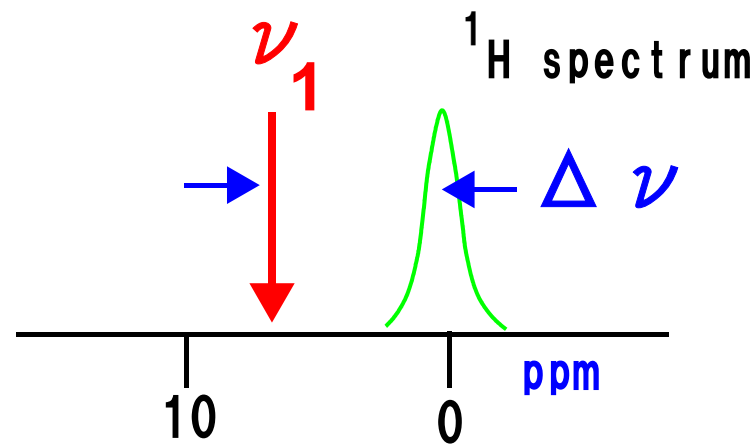
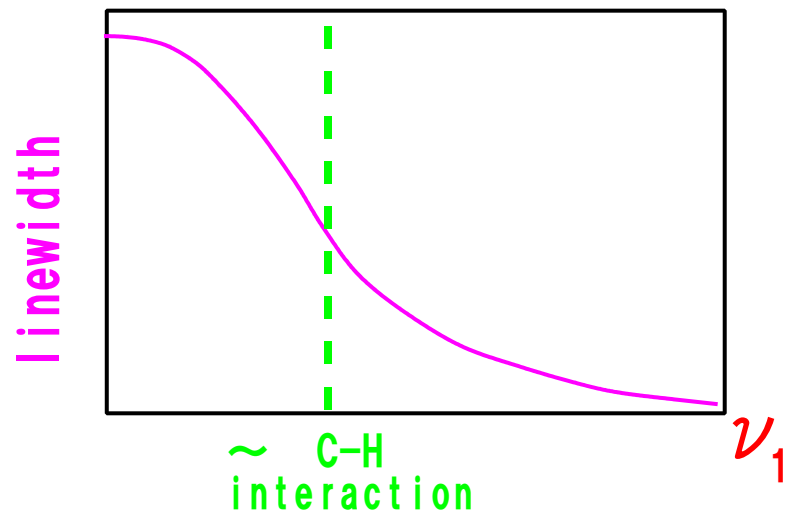


$$\begin{aligned} \nu_1 &\gg \text{}^1\text{H}-^{13}\text{C} \text{ dipolar coupling} \\ &\gg \sim 40 \text{ kHz} \end{aligned}$$

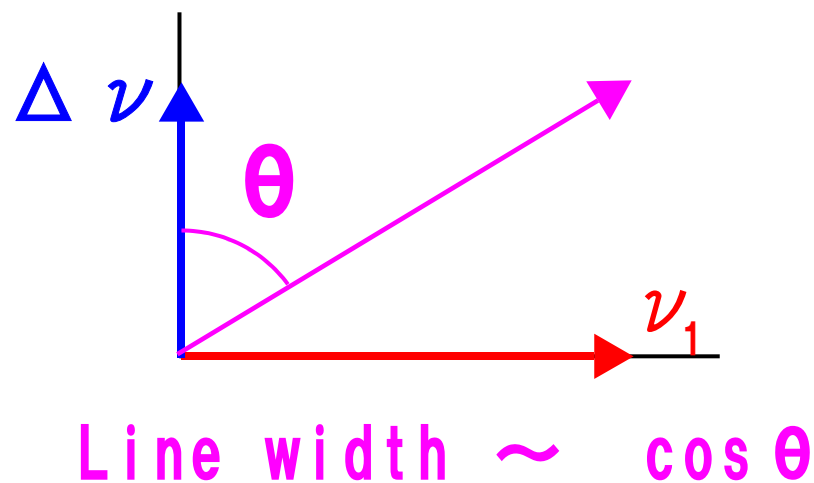
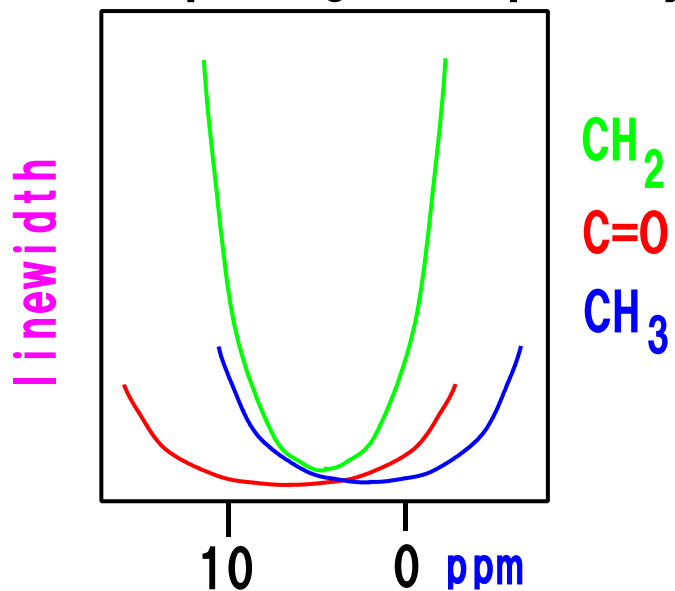
$$\begin{aligned} &d I_z S_z \\ &\downarrow \text{irradiation on } I \\ &d (I_z \cos \nu_1 t + I_z \sin \nu_1 t) S_z \\ &\downarrow \\ &0 \end{aligned}$$

Decoupling efficiency

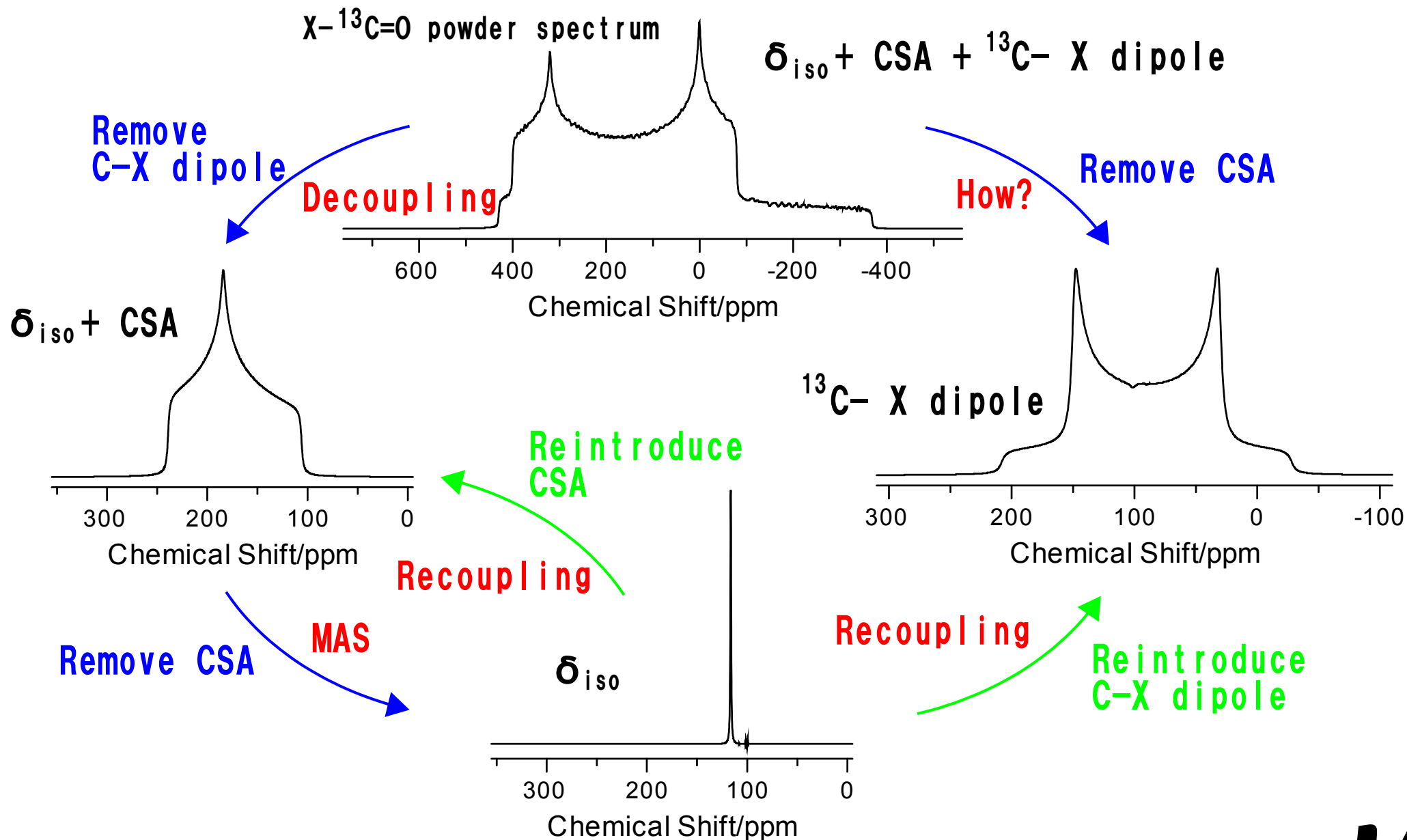
Decoupling power



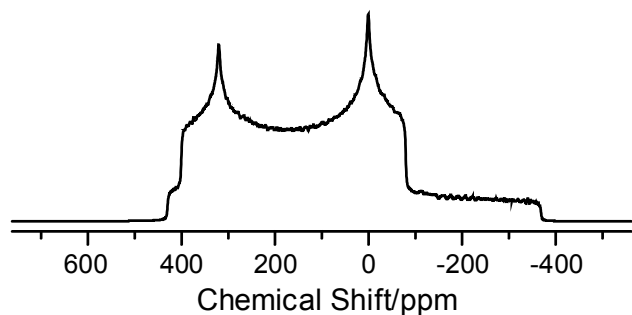
Decoupling frequency



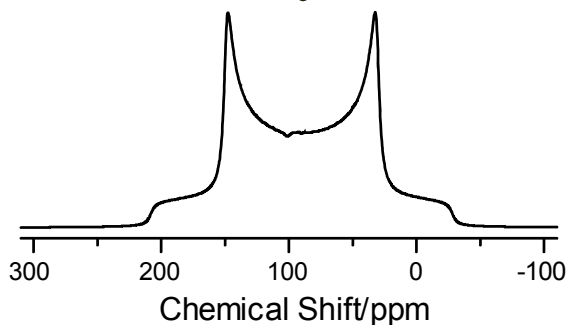
Decoupling and recoupling



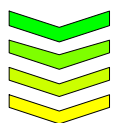
A simple case: a two I-S spin system



$\delta_{iso} + CSA + I-S$ dipole



I-S dipole



I-S distance

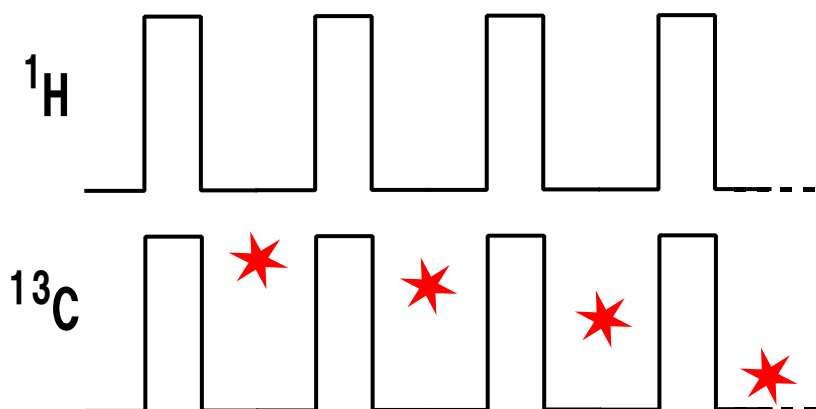
$$(\delta_{iso} + \delta_{csa}) S_z + d I_z S_z \quad (1)$$

π pulse to S&I \downarrow $S_z \rightarrow -S_z$
 $I_z \rightarrow -I_z$

$$-(\delta_{iso} + \delta_{csa}) S_z + d I_z S_z \quad (2)$$

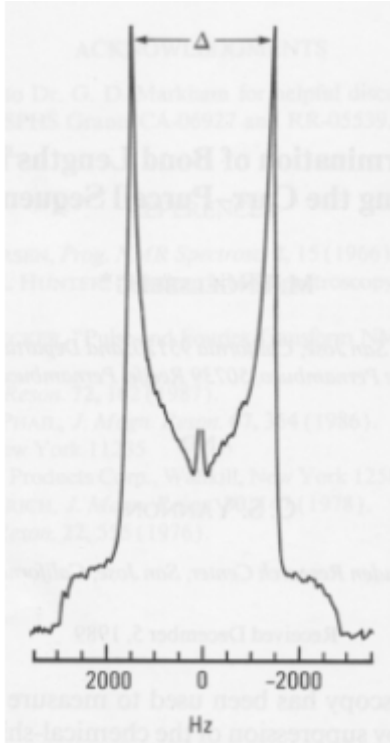
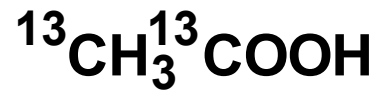
$$\frac{(1) + (2)}{2} = d I_z S_z$$

π pulse trains to S&I



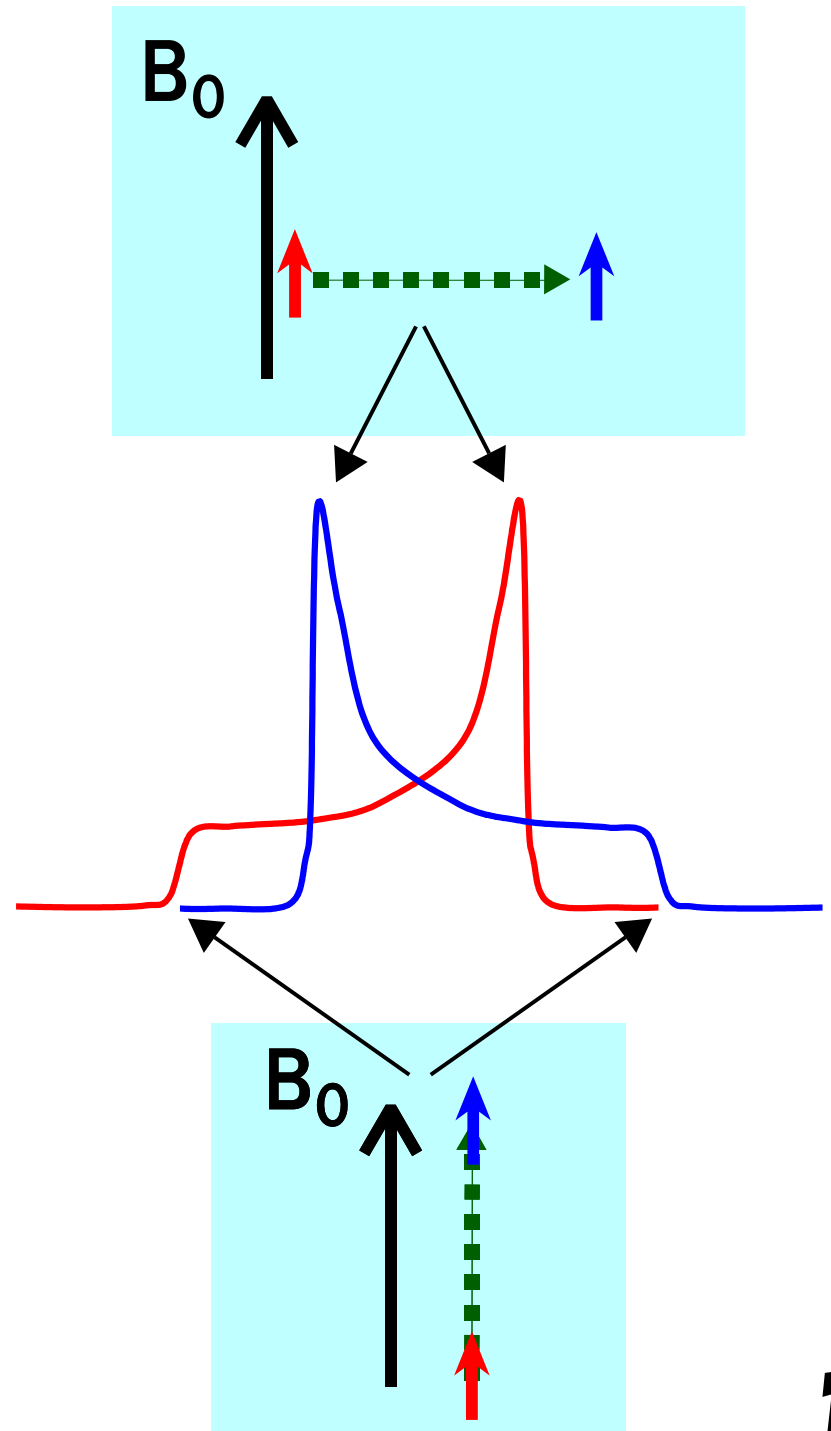
★: Observe stroboscopically

Dipolar powder pattern



$$\Delta = d_0(3\cos^2\theta - 1) / r^3$$

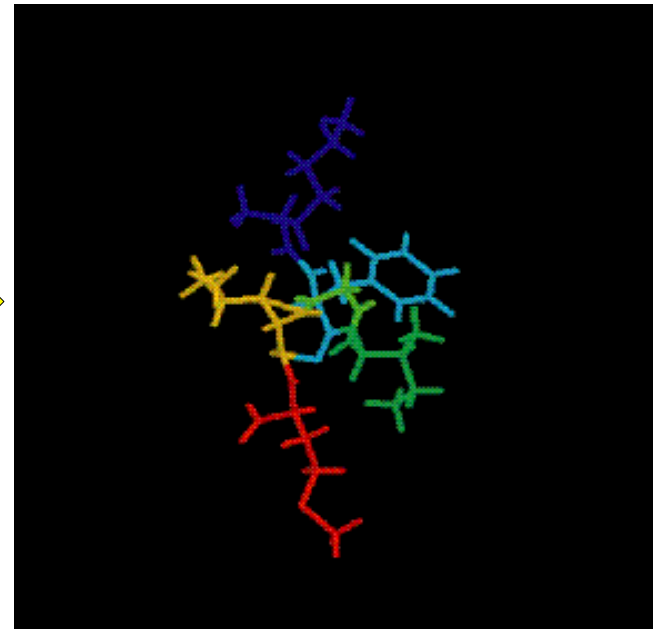
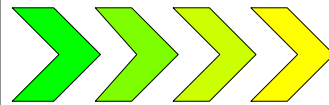
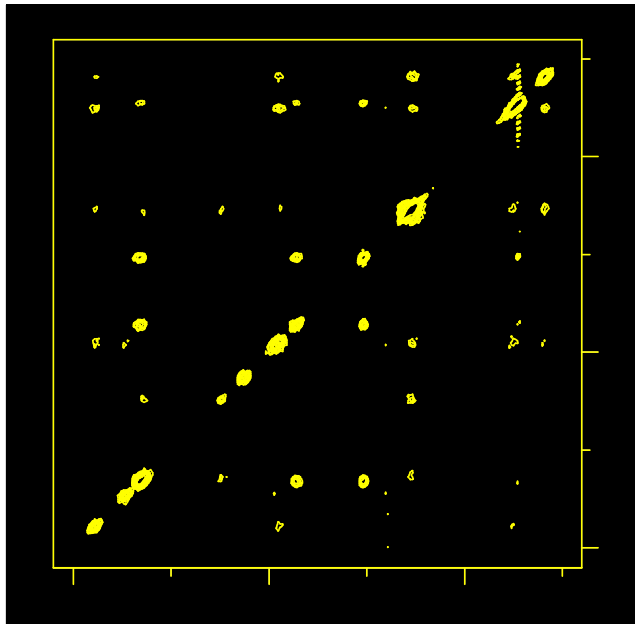
M. Engelsberg, C.S. Yannoni,
J. Magn. Reson., 88, 393 (1990)



Structural determination by solid NMR

Resolution of ^1H resonances is too bad....

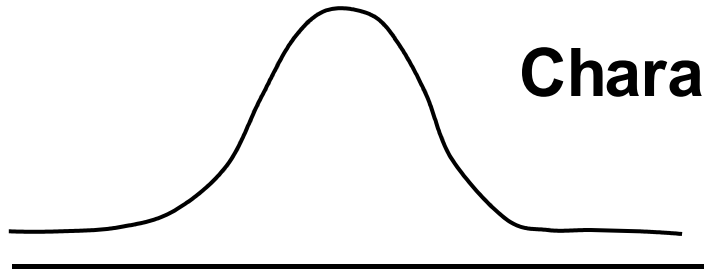
We replace ^{12}C and ^{14}N by ^{13}C and ^{15}N to observed NMR...



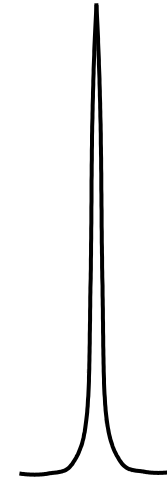
Uniform ^{13}C labeling

1) Spectral overlap due to anisotropic line broadening

Chemical shift anisotropy & Dipole-dipole coupling

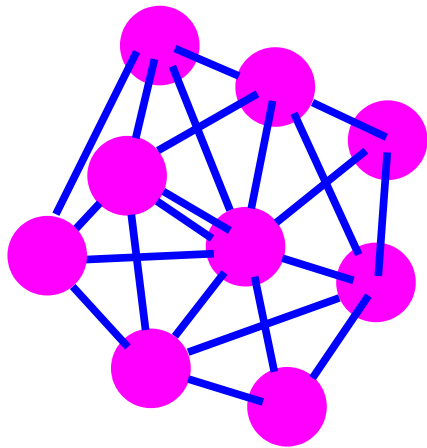


MAS

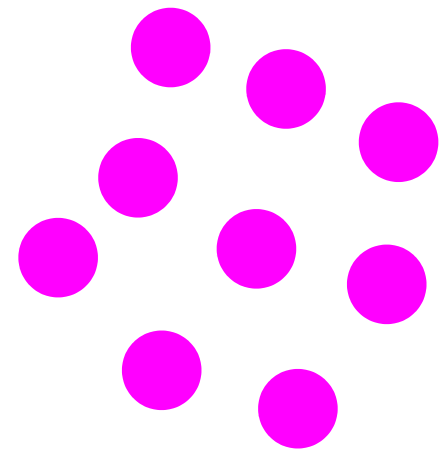


2) Many spin problem

Remove CSA & dipole-dipole couplings



$n\text{C}_2$



Recoupling under MAS

Spin interaction $\mathbf{H} \sim$ [Space part] \times [Spin part]

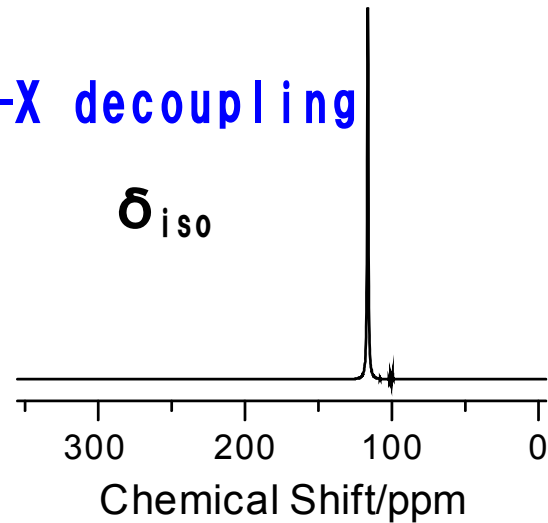
Space part \sim $\cos \nu_R t, \cos 2 \nu_R t \xrightarrow{\text{time average}} 0$
MAS

Spin part $\xrightarrow{\text{rf}}$ $\mathbf{S}(t)$

$$\int_0^{\tau} \mathbf{H}(t) dt \xrightarrow{\quad} \neq 0 \quad \text{Recoupling}$$

Dipolar recoupling under MAS

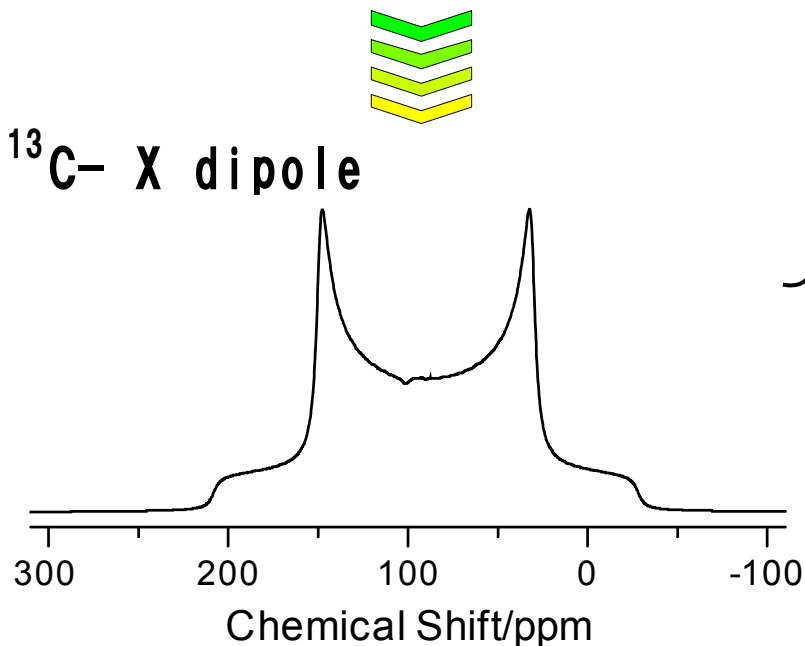
MAS / C-X decoupling



$$\mathbf{H}_d = d(t) (I_z \cos \nu_1 t + I_x \sin \nu_1 t) S_z$$

$$d(t) = C_1 \cos(\nu_R t + \gamma) + C_2 \cos(2\nu_R t + 2\gamma)$$

^{13}C - X dipole

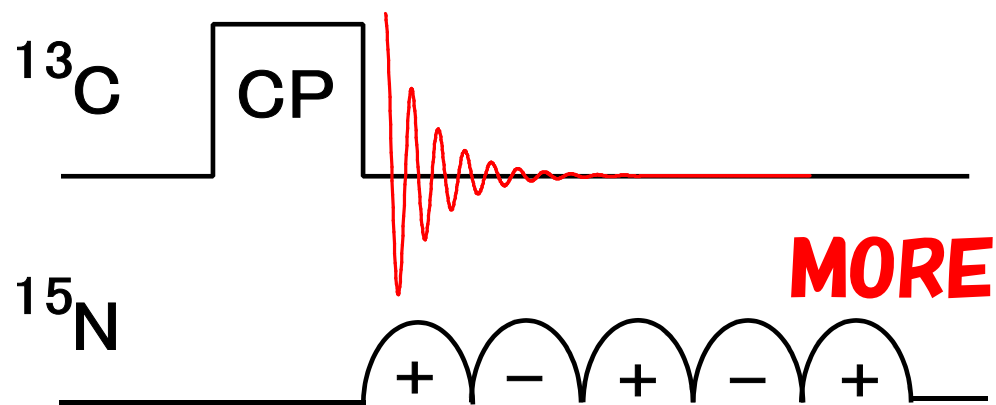


$$\int_0^{\tau} \mathbf{H}_d(t) dt \xrightarrow{\nu_1 \gg \nu_R} 0 \quad \text{Decoupling}$$

$$\xrightarrow{\nu_1 = \nu_R} \neq 0 \quad \text{Recoupling}$$

(The rotary-resonance condition)

eg. $^{13}\text{C}-^{15}\text{N}$ recoupling under MAS

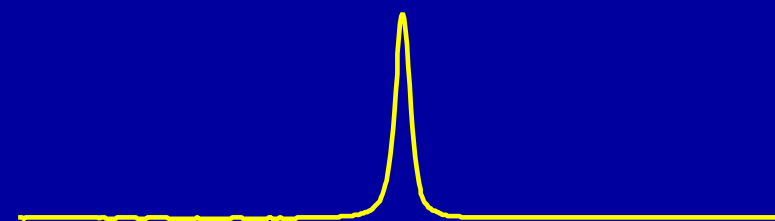


$$H_D^{\text{CN}}(t) = d(t) I_z S_z$$

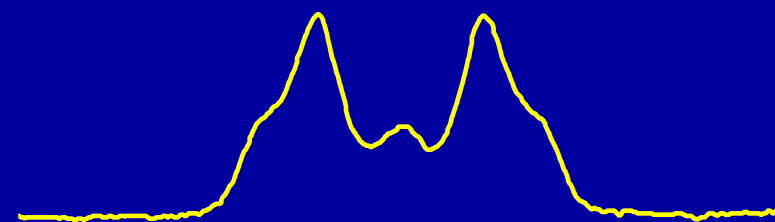
$$H_{\text{rf}} = H_1 \cos(\omega t) S_x$$

$$\omega = \omega_{\text{MAS}} \times 1 \text{ or } 2$$

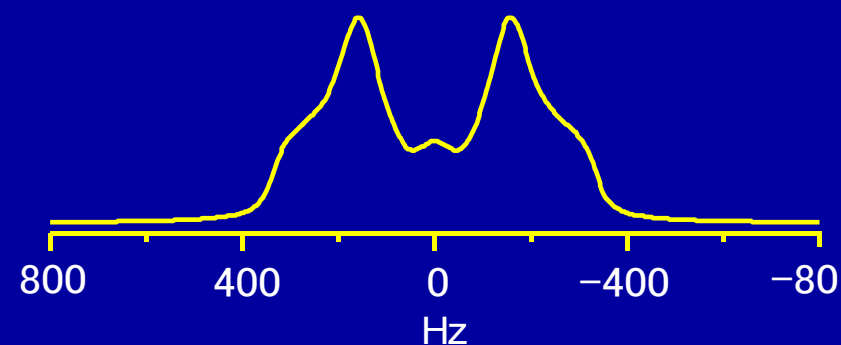
(a) conventional CPMAS



(b) MORE experimental

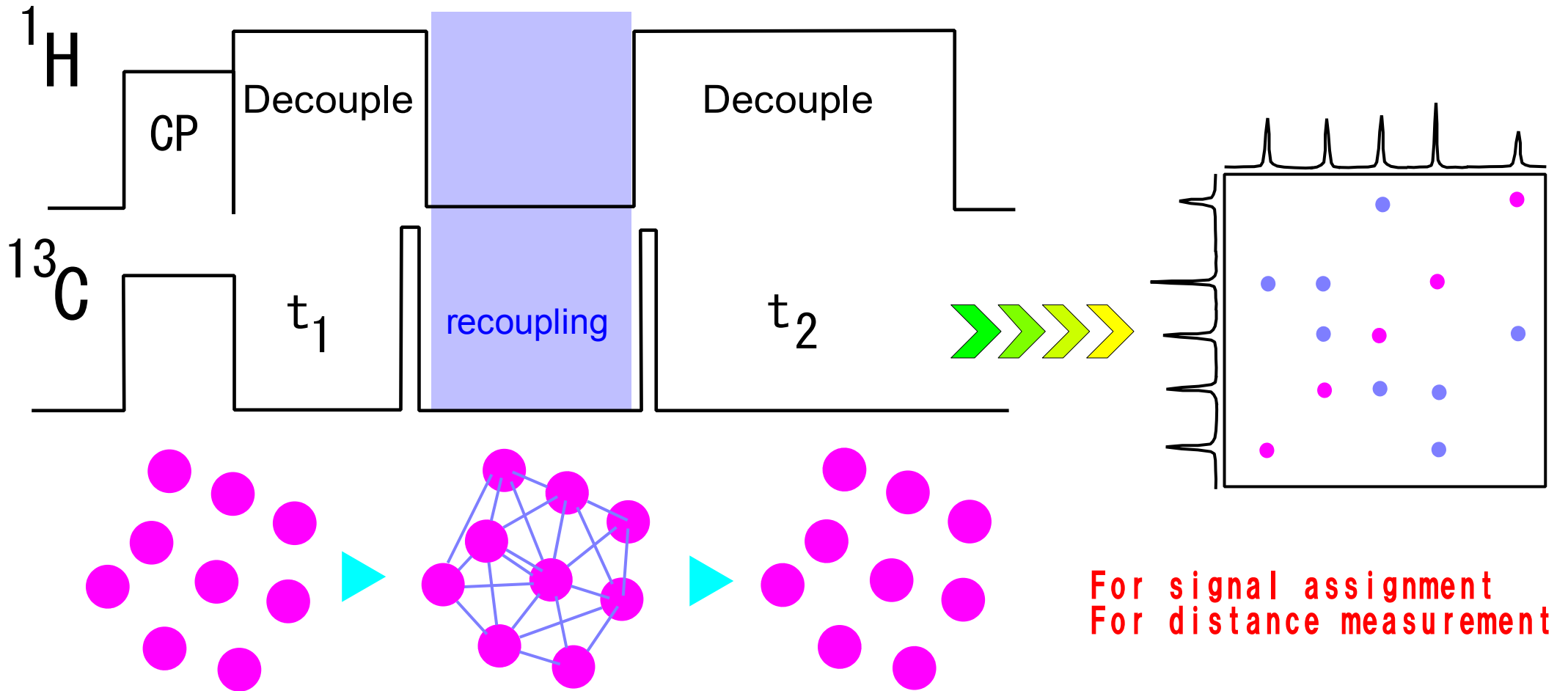


(c) MORE simulation

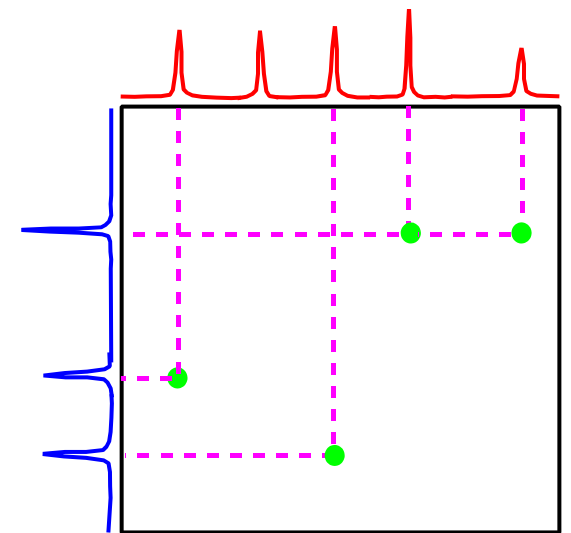
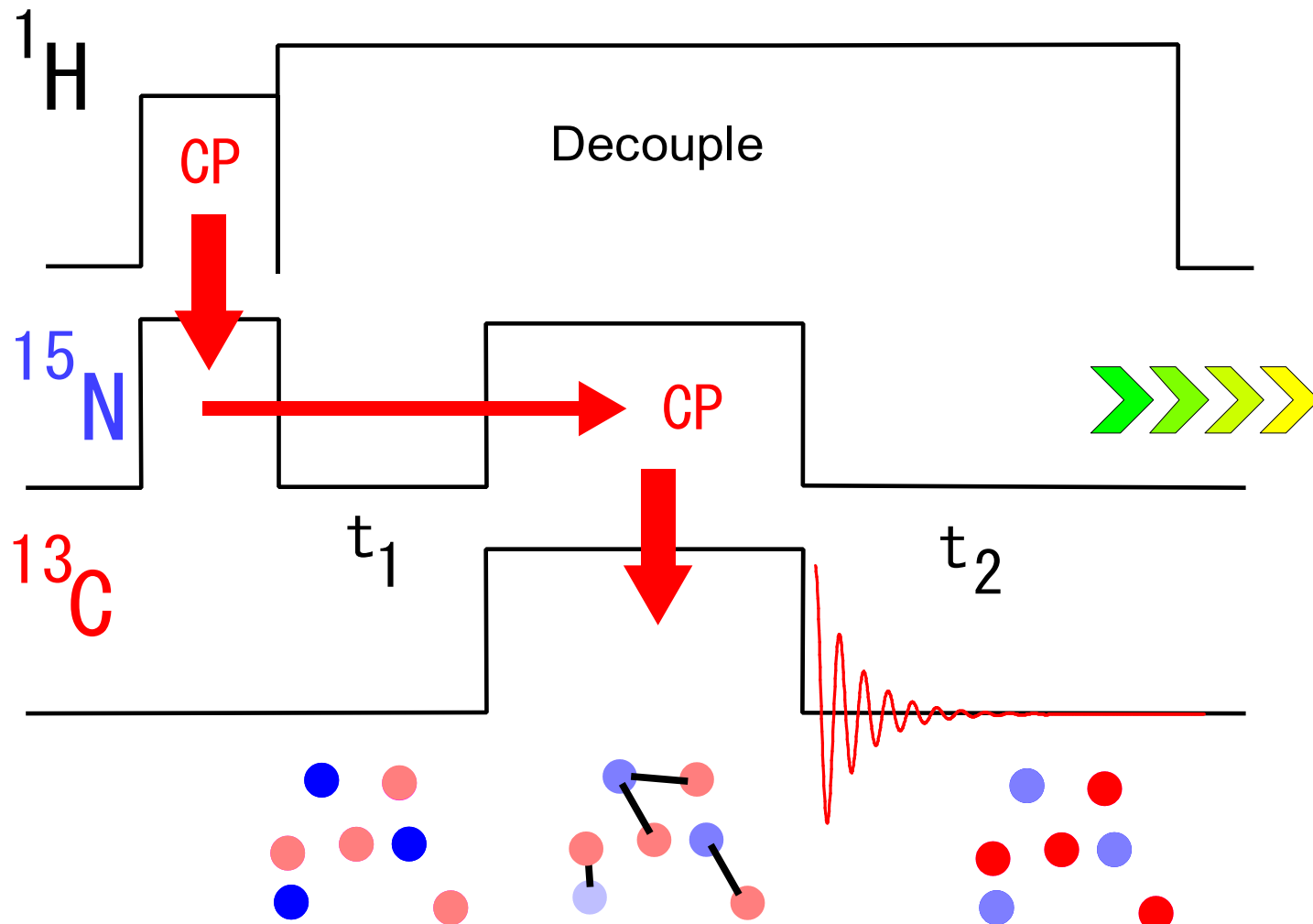


$[2-^{13}\text{C}, ^{15}\text{N}]$ glycine

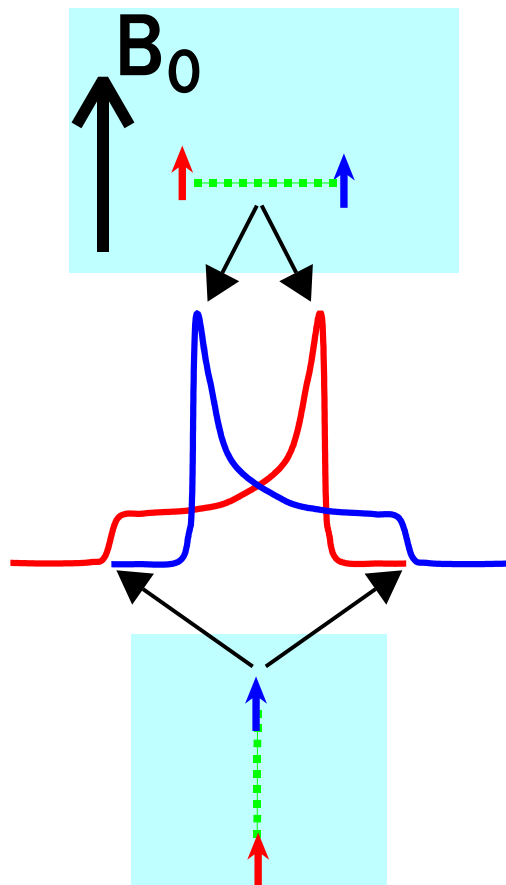
A 2D ^{13}C - ^{13}C exchange experiment



A 2D ^{15}N - ^{13}C correlation experiment



Angles by solid NMR



A dipolar powder pattern

